

# Additional Issues: Random effects diagnostics, multiple comparisons

Austin F. Frank, T. Florian Jaeger

April 30, 2009

## Visualizing and testing random effects

### Post hoc comparisons

# The dative dataset

- ▶ Original analysis in Bresnan *et al* (2007)
- ▶ Data obtained from `languageR` (Baayen 2008)
- ▶ “Data describing the realization of the dative as NP or PP in the Switchboard corpus and the Treebank Wall Street Journal collection.”
- ▶ 3,263 observations, 74% NP realization
- ▶ 75 verbs

# The dative dataset

- ▶ Original analysis in Bresnan *et al* (2007)
- ▶ Data obtained from languageR (Baayen 2008)
- ▶ “Data describing the realization of the dative as NP or PP in the Switchboard corpus and the Treebank Wall Street Journal collection.”
- ▶ 3,263 observations, 74% NP realization
- ▶ 75 verbs

# The dative dataset

- ▶ Original analysis in Bresnan *et al* (2007)
- ▶ Data obtained from languageR (Baayen 2008)
- ▶ “Data describing the realization of the dative as NP or PP in the Switchboard corpus and the Treebank Wall Street Journal collection.”
- ▶ 3,263 observations, 74% NP realization
- ▶ 75 verbs

# The dative dataset

- ▶ Original analysis in Bresnan *et al* (2007)
- ▶ Data obtained from languageR (Baayen 2008)
- ▶ “Data describing the realization of the dative as NP or PP in the Switchboard corpus and the Treebank Wall Street Journal collection.”
- ▶ 3,263 observations, 74% NP realization
- ▶ 75 verbs

# The dative dataset

- ▶ Original analysis in Bresnan *et al* (2007)
- ▶ Data obtained from languageR (Baayen 2008)
- ▶ “Data describing the realization of the dative as NP or PP in the Switchboard corpus and the Treebank Wall Street Journal collection.”
- ▶ 3,263 observations, 74% NP realization
- ▶ 75 verbs

# Random intercept model

```
> dative.lmer <- lmer(RealizationOfRecipient ~  
+   AccessOfRec + AnimacyOfRec + LengthOfRecipient +  
+   AccessOfTheme + AnimacyOfTheme + LengthOfTheme +  
+   PronomOfTheme + DefinOfTheme + SemanticClass + Modality +  
+   (1 | Verb),  
+   data = dative, family = ``binomial``)
```

Random effects:

Groups Name	Variance	Std.Dev.
Verb (Intercept)	4.3982	2.0972

Number of obs: 3263, groups: Verb, 75

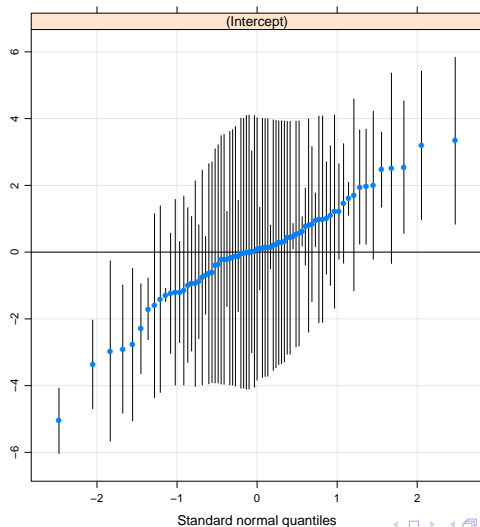
# Random intercept model: fixed effects

## Fixed effects:

	Estimate	Std. Error	z value	Pr(> z )	
(Intercept)	1.29306	0.65005	1.989	0.0467	*
AccessOfRecgiven	-2.46128	0.17761	-13.858	< 2e-16	***
AccessOfRecnew	0.12462	0.24422	0.510	0.6099	
AnimacyOfRecinanimate	2.24226	0.25864	8.669	< 2e-16	***
LengthOfRecipient	0.41486	0.04754	8.727	< 2e-16	***
AccessOfThemegiven	1.50539	0.25504	5.903	3.58e-09	***
AccessOfThemew	-0.41979	0.19067	-2.202	0.0277	*
AnimacyOfThemeinanimate	-0.86355	0.48283	-1.789	0.0737	.
LengthOfTheme	-0.23354	0.02766	-8.442	< 2e-16	***
PronomOfThemeprenominal	2.20502	0.24624	8.955	< 2e-16	***
DefinOfThemeindefinite	-0.93294	0.19024	-4.904	9.39e-07	***
SemanticClassc	0.38583	0.34928	1.105	0.2693	
SemanticClassf	0.02208	0.57970	0.038	0.9696	
SemanticClassp	-3.77591	1.47575	-2.559	0.0105	*
SemanticClasst	0.31043	0.20895	1.486	0.1374	
Modalitywritten	0.85012	0.18536	4.586	4.51e-06	***

# Random intercepts: QQ plot

```
> library(lattice)
> dative.ranef <- ranef(dative.lmer, postVar = TRUE)
> qqmath(dative.ranef)
```

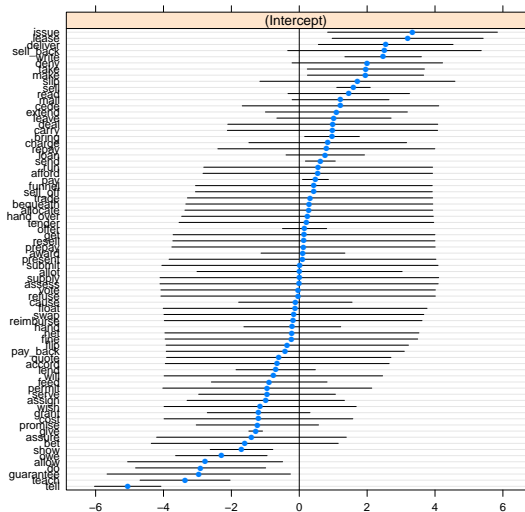


# Random intercepts: caterpillar plot

```
> library(lattice)
> dative.ranef <- ranef(dative.lmer, postVar = TRUE)
> dotplot(dative.ranef)
```

Visualizing and  
testing random  
effects

Post hoc  
comparisons



# Random slope model

```
> dative.lmer.slope <- lmer(RealizationOfRecipient ~  
+   AccessOfRec + AnimacyOfRec + LengthOfRecipient +  
+   AccessOfTheme + AnimacyOfTheme + LengthOfTheme +  
+   PronomOfTheme + DefinOfTheme + SemanticClass + Modality +  
+   (1 + Modality | Verb),  
  data = dative, family = ``binomial``)
```

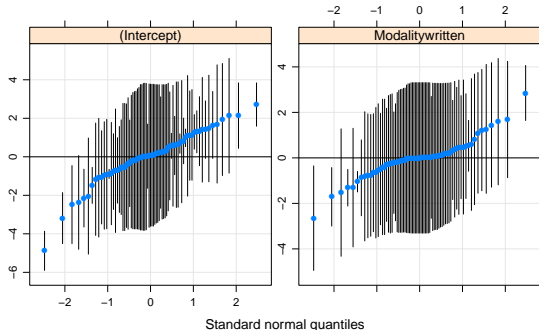
Random effects:

Groups Name	Variance	Std.Dev.	Corr
Verb (Intercept)	3.8098	1.9519	
Modalitywritten	2.8482	1.6877	0.000

Number of obs: 3263, groups: Verb, 75

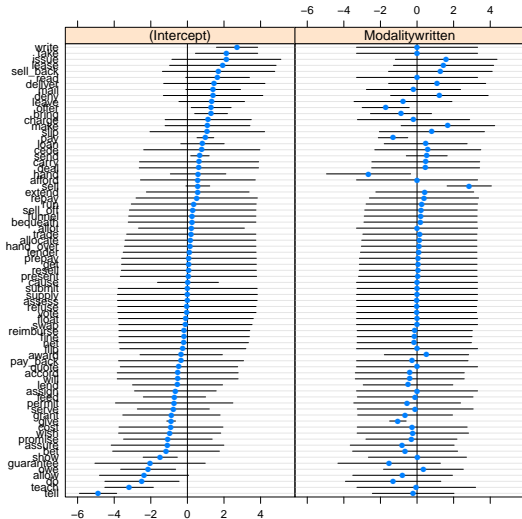
# Random slope: QQ plot

```
> library(lattice)
> dative.ranef <- ranef(dative.lmer.slope, postVar = TRUE)
> qqmath(dative.ranef)
```



# Random slope: caterpillar plot

```
> library(lattice)
> dative.ranef <- ranef(dative.lmer.slope, postVar = TRUE)
> dotplot(dative.ranef)
```



# Model comparison

```
> anova(dative.lmer, dative.lmer.slope)

              Df      AIC      BIC  logLik  Chisq Chi Df Pr(>Chisq)
dative.lmer      17 1561.05 1664.59 -763.52
dative.lmer.slope 19 1524.71 1640.42 -743.35 40.344      2 1.735e-09 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

We conclude that a random slope term for modality significantly improves the fit of the model to data based on a likelihood ratio test ( $\chi^2_{\Delta\lambda}(2) = 40.3, p < .0001$ )

Visualizing and testing random effects

**Post hoc comparisons**

# Initial considerations

- ▶ Preferred method for hypothesis testing on regression parameters is to include relevant orthogonal contrasts in the original model
- ▶ Whether doing planned or *post hoc* comparisons on linear mixed models, distributional assumptions for hypothesis testing are murky at best (*c.f.* <http://wiki.r-project.org/rwiki/doku.php?id=guides:lmer-tests>, <https://stat.ethz.ch/pipermail/r-help/2006-May/094765.html>)
- ▶ Hypothesis testing on regression parameters for generalized linear mixed models depends on the data matching distributional assumptions. Over- or underdispersion in the data makes standard error calculations on regression coefficients unreliable.
- ▶ Multiplicity corrections may be unnecessary, depending on your understanding of hypothesis testing (Gelman, Hill, & Yajima, in prep)
- ▶ “The difference between ‘significant’ and ‘not significant’ is not itself statistically significant” (Gelman & Stern 2006)

# Initial considerations

- ▶ Preferred method for hypothesis testing on regression parameters is to include relevant orthogonal contrasts in the original model
- ▶ Whether doing planned or *post hoc* comparisons on linear mixed models, distributional assumptions for hypothesis testing are murky at best (*c.f.* <http://wiki.r-project.org/rwiki/doku.php?id=guides:lmer-tests>, <https://stat.ethz.ch/pipermail/r-help/2006-May/094765.html>)
- ▶ Hypothesis testing on regression parameters for generalized linear mixed models depends on the data matching distributional assumptions. Over- or underdispersion in the data makes standard error calculations on regression coefficients unreliable.
- ▶ Multiplicity corrections may be unnecessary, depending on your understanding of hypothesis testing (Gelman, Hill, & Yajima, in prep)
- ▶ “The difference between ‘significant’ and ‘not significant’ is not itself statistically significant” (Gelman & Stern 2006)

# Initial considerations

- ▶ Preferred method for hypothesis testing on regression parameters is to include relevant orthogonal contrasts in the original model
- ▶ Whether doing planned or *post hoc* comparisons on linear mixed models, distributional assumptions for hypothesis testing are murky at best (*c.f.* <http://wiki.r-project.org/rwiki/doku.php?id=guides:lmer-tests>, <https://stat.ethz.ch/pipermail/r-help/2006-May/094765.html>)
- ▶ Hypothesis testing on regression parameters for generalized linear mixed models depends on the data matching distributional assumptions. Over- or underdispersion in the data makes standard error calculations on regression coefficients unreliable.
- ▶ Multiplicity corrections may be unnecessary, depending on your understanding of hypothesis testing (Gelman, Hill, & Yajima, in prep)
- ▶ “The difference between ‘significant’ and ‘not significant’ is not itself statistically significant” (Gelman & Stern 2006)

# Initial considerations

- ▶ Preferred method for hypothesis testing on regression parameters is to include relevant orthogonal contrasts in the original model
- ▶ Whether doing planned or *post hoc* comparisons on linear mixed models, distributional assumptions for hypothesis testing are murky at best (*c.f.*  
<http://wiki.r-project.org/rwiki/doku.php?id=guides:lmer-tests>,  
<https://stat.ethz.ch/pipermail/r-help/2006-May/094765.html>)
- ▶ Hypothesis testing on regression parameters for generalized linear mixed models depends on the data matching distributional assumptions. Over- or underdispersion in the data makes standard error calculations on regression coefficients unreliable.
- ▶ Multiplicity corrections may be unnecessary, depending on your understanding of hypothesis testing (Gelman, Hill, & Yajima, in prep)
- ▶ “The difference between ‘significant’ and ‘not significant’ is not itself statistically significant” (Gelman & Stern 2006)

# Initial considerations

- ▶ Preferred method for hypothesis testing on regression parameters is to include relevant orthogonal contrasts in the original model
- ▶ Whether doing planned or *post hoc* comparisons on linear mixed models, distributional assumptions for hypothesis testing are murky at best (*c.f.*  
<http://wiki.r-project.org/rwiki/doku.php?id=guides:lmer-tests>,  
<https://stat.ethz.ch/pipermail/r-help/2006-May/094765.html>)
- ▶ Hypothesis testing on regression parameters for generalized linear mixed models depends on the data matching distributional assumptions. Over- or underdispersion in the data makes standard error calculations on regression coefficients unreliable.
- ▶ Multiplicity corrections may be unnecessary, depending on your understanding of hypothesis testing (Gelman, Hill, & Yajima, in prep)
- ▶ “The difference between ‘significant’ and ‘not significant’ is not itself statistically significant” (Gelman & Stern 2006)

# Post hoc comparisons: motivations

You may want to use *post hoc* comparisons if you ...

- ▶ are interested in testing hypotheses about specific combinations of levels in a categorical predictor
- ▶ can't include all comparisons of interest in planned contrasts (e.g. because of collinearity)
- ▶ want to evaluate impact of different contrast coding schemes, balance assumptions
- ▶ seek to control **family-wise error rate** (probability of rejecting at least one true null hypothesis from a set of null hypotheses)

# Post hoc comparisons: motivations

You may want to use *post hoc* comparisons if you . . .

- ▶ are interested in testing hypotheses about specific combinations of levels in a categorical predictor
- ▶ can't include all comparisons of interest in planned contrasts (e.g. because of collinearity)
- ▶ want to evaluate impact of different contrast coding schemes, balance assumptions
- ▶ seek to control **family-wise error rate** (probability of rejecting at least one true null hypothesis from a set of null hypotheses)

# Post hoc comparisons: motivations

You may want to use *post hoc* comparisons if you . . .

- ▶ are interested in testing hypotheses about specific combinations of levels in a categorical predictor
- ▶ can't include all comparisons of interest in planned contrasts (*e.g.* because of collinearity)
- ▶ want to evaluate impact of different contrast coding schemes, balance assumptions
- ▶ seek to control **family-wise error rate** (probability of rejecting at least one true null hypothesis from a set of null hypotheses)

# Post hoc comparisons: motivations

You may want to use *post hoc* comparisons if you ...

- ▶ are interested in testing hypotheses about specific combinations of levels in a categorical predictor
- ▶ can't include all comparisons of interest in planned contrasts (*e.g.* because of collinearity)
- ▶ want to evaluate impact of different contrast coding schemes, balance assumptions
- ▶ seek to control **family-wise error rate** (probability of rejecting at least one true null hypothesis from a set of null hypotheses)

# Post hoc comparisons: motivations

You may want to use *post hoc* comparisons if you ...

- ▶ are interested in testing hypotheses about specific combinations of levels in a categorical predictor
- ▶ can't include all comparisons of interest in planned contrasts (e.g. because of collinearity)
- ▶ want to evaluate impact of different contrast coding schemes, balance assumptions
- ▶ seek to control **family-wise error rate** (probability of rejecting at least one true null hypothesis from a set of null hypotheses)

# Implementing post hoc comparisons

- ▶ Use the `multcomp` package in R (Hothorn 2006, 2008)
- ▶ Two orthogonal issues:
  1. Specifying contrasts
  2. Multiple comparisons

# Implementing post hoc comparisons

Additional Issues

AF Frank, TF  
Jaeger

Visualizing and  
testing random  
effects

Post hoc  
comparisons

- ▶ Use the `multcomp` package in R (Hothorn 2006, 2008)
- ▶ Two orthogonal issues:
  1. Specifying contrasts
  2. Multiplicity corrections

# Implementing post hoc comparisons

Additional Issues

AF Frank, TF  
Jaeger

Visualizing and  
testing random  
effects

Post hoc  
comparisons

- ▶ Use the `multcomp` package in R (Hothorn 2006, 2008)
- ▶ Two orthogonal issues:
  1. Specifying contrasts
  2. Multiplicity corrections

# Implementing post hoc comparisons

Additional Issues

AF Frank, TF  
Jaeger

Visualizing and  
testing random  
effects

Post hoc  
comparisons

- ▶ Use the `multcomp` package in R (Hothorn 2006, 2008)
- ▶ Two orthogonal issues:
  1. Specifying contrasts
  2. Multiplicity corrections

# Specifying contrasts in multcomp

## Three methods

1. Named contrast coding scheme (e.g. Dunnett, Tukey, Helmert (see p. 648, Bretz *et al*, 2001))
2. String specification ("A - B = 0")
3. Build arbitrary contrast matrix from scratch

# Specifying contrasts in multcomp

## Three methods

1. Named contrast coding scheme (e.g. Dunnett, Tukey, Helmert (see p. 648, Bretz *et al*, 2001))
2. String specification ("A - B = 0")
3. Build arbitrary contrast matrix from scratch

# Specifying contrasts in multcomp

## Three methods

1. Named contrast coding scheme (e.g. Dunnett, Tukey, Helmert (see p. 648, Bretz *et al*, 2001))
2. String specification ("A - B = 0")
3. Build arbitrary contrast matrix from scratch

# Specifying contrasts in multcomp

## Three methods

1. Named contrast coding scheme (e.g. Dunnett, Tukey, Helmert (see p. 648, Bretz *et al*, 2001))
2. String specification ("A - B = 0")
3. Build arbitrary contrast matrix from scratch

# multcomp warning

multcomp contrast matrices are transposed from normal R contrast matrices

```
> contr.sum(3)
  [,1] [,2]
1    1    0
2    0    1
3   -1   -1

> contrMat(c(1,1,1), ``Dunnett``)
Multiple Comparisons of Means: Dunnett Contrasts

      1 2 3
2 - 1 -1 1 0
3 - 1 -1 0 1
```

Use `t()` to change between orientations

# multcomp warning

multcomp contrast matrices are transposed from normal R contrast matrices

```
> contr.sum(3)
  [,1] [,2]
1    1    0
2    0    1
3   -1   -1
> contrMat(c(1,1,1), ``Dunnett``)
Multiple Comparisons of Means: Dunnett Contrasts
      1 2 3
2 - 1 -1 1 0
3 - 1 -1 0 1
```

Use `t()` to change between orientations

# Worked example

```
> dative.lmer.access <-  
+ lmer(RealizationOfRecipient ~  
+      -1 + AccessOfTheme +  
+      (0 + AccessOfTheme | Verb),  
+      dative,  
+      family = ``binomial``)
```

Random effects:

Groups	Name	Variance	Std.Dev.	Corr
Verb	AccessOfThemeaccessible	3.6343	1.9064	
	AccessOfThemegiven	4.0210	2.0053	0.938
	AccessOfThemeneu	5.3445	2.3118	0.929 0.919

Number of obs: 3263, groups: Verb, 75

Fixed effects:

	Estimate	Std. Error	z value	Pr(> z )	
AccessOfThemeaccessible	-0.8172	0.2900	-2.818	0.004836	**
AccessOfThemegiven	1.3781	0.3590	3.839	0.000124	***
AccessOfThemeneu	-1.0370	0.3660	-2.833	0.004609	**

Aside: can you spot an error in this model specification?

# Collinearity in accessibility model

```
Correlation of Fixed Effects:
              AccssOfThmc AccssOfThmg
AccssOfThmg  0.659
AccssOfThmn  0.697          0.593

> collin.fnc(data.frame(dative.lmer.access@X))$cnumber
[1] 1.647076e+14
```

# Treatment (dummy) coding

```
> K <- diag(length(fixef(dative.lmer.access)))  
> rownames(K) <- c(``Accessible``, ``Given``, ``New``)  
> colnames(K) <- c(``Accessible``, ``Given``, ``New``)
```

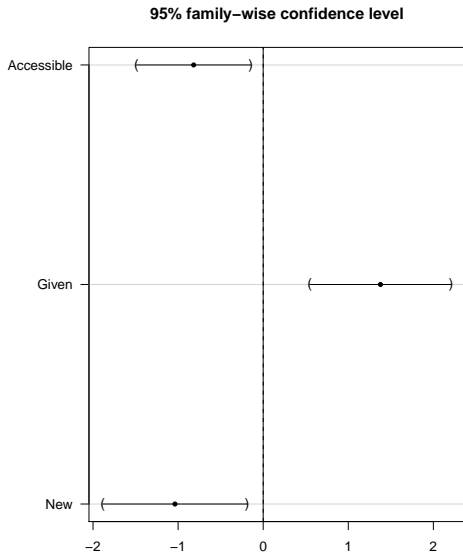
	Accessible	Given	New
Accessible	1	0	0
Given	0	1	0
New	0	0	1

# Treatment effects

```
> plot(confint(glht(dative.lmer.access, linfct = K)))
```

Visualizing and  
testing random  
effects

Post hoc  
comparisons



# Contrast (Dunnett, sum) coding

```
> K <- rbind(K,  
+           ``Accessible - New`` = c(1, 0, -1),  
+           ``Given - New`` = c(0, 1, -1))
```

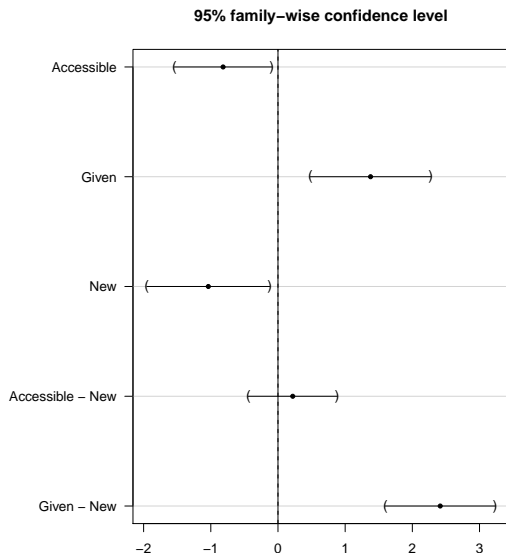
	Accessible	Given	New
Accessible	1	0	0
Given	0	1	0
New	0	0	1
Accessible - New	1	0	-1
Given - New	0	1	-1

# Contrast effects

```
> plot(confint(glht(dative.lmer.access, linfct = K)))
```

Visualizing and  
testing random  
effects

Post hoc  
comparisons



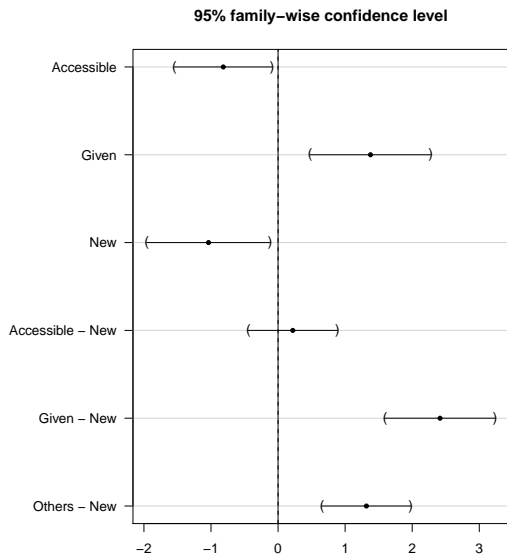
# Arbitrary combinations

```
> K <- rbind(K, ``Others - New'' = c(.5, .5, -1))
```

	Accessible	Given	New
Accessible	1.0	0.0	0
Given	0.0	1.0	0
New	0.0	0.0	1
Accessible - New	1.0	0.0	-1
Given - New	0.0	1.0	-1
Others - New	0.5	0.5	-1

# Arbitrary comparison

```
> plot(confint(glht(dative.lmer.access, linfct = K)))
```



# Hidden assumption: balanced data

The weights assigned in the contrasts coded tests and the arbitrary test assume that we have balanced data. If this assumption is violated, one condition will contribute more to the test than the others.

Is the accessibility data balanced?

```
> prop.table(table(dative$AccessOfRec))
```

accessible	given	new
0.1884769	0.7054857	0.1060374

Discussion question / exercise: can we still use these coding strategies with unbalanced data? What should we change?

# Multiplicity corrections

- ▶ Adjust criterion for rejecting  $H_0^i$  as a function of the number of hypotheses being tested.
- ▶ Suggested if analysis is being treated as “simultaneous inference”.
- ▶ Correction procedures fall into two categories: **single step** and **stepwise**. Stepwise procedures require that all combinations of hypotheses including a particular  $H_0^i$  before it can be rejected.

# Multiplicity corrections

- ▶ Adjust criterion for rejecting  $H_0^i$  as a function of the number of hypotheses being tested.
- ▶ Suggested if analysis is being treated as “simultaneous inference”.
- ▶ Correction procedures fall into two categories: **single step** and **stepwise**. Stepwise procedures require that all combinations of hypotheses including a particular  $H_0^i$  before it can be rejected.

# Multiplicity corrections

- ▶ Adjust criterion for rejecting  $H_0^i$  as a function of the number of hypotheses being tested.
- ▶ Suggested if analysis is being treated as “simultaneous inference”.
- ▶ Correction procedures fall into two categories: **single step** and **stepwise**. Stepwise procedures require that all combinations of hypotheses including a particular  $H_0^i$  before it can be rejected.

# No correction

```
> summary(glht(dative.lmer.access, linfct = K), test = adjusted(`none`))
```

Simultaneous Tests for General Linear Hypotheses

```
Fit: glmer(formula = RealizationOfRecipient ~ -1 + AccessOfTheme +  
(0 + AccessOfTheme | Verb), data = dative, family = `binomial`)
```

Linear Hypotheses:

	Estimate	Std. Error	z value	Pr(> z )	
Accessible == 0	-0.8172	0.2900	-2.818	0.004836	**
Given == 0	1.3781	0.3590	3.839	0.000124	***
New == 0	-1.0370	0.3660	-2.833	0.004609	**
Accessible - New == 0	0.2198	0.2646	0.831	0.406106	
Given - New == 0	2.4151	0.3272	7.381	1.57e-13	***
Others - New == 0	1.3174	0.2638	4.995	5.89e-07	***

---

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
(Adjusted p values reported -- none method)
```

# Bonferroni correction

```
> summary(glht(dative.lmer.access, linfct = K), test = adjusted(``bon``))
```

## Simultaneous Tests for General Linear Hypotheses

```
Fit: glmer(formula = RealizationOfRecipient ~ -1 + AccessOfTheme +  
(0 + AccessOfTheme | Verb), data = dative, family = ``binomial``)
```

### Linear Hypotheses:

	Estimate	Std. Error	z value	Pr(> z )	
Accessible == 0	-0.8172	0.2900	-2.818	0.029017	*
Given == 0	1.3781	0.3590	3.839	0.000742	***
New == 0	-1.0370	0.3660	-2.833	0.027655	*
Accessible - New == 0	0.2198	0.2646	0.831	1.000000	
Given - New == 0	2.4151	0.3272	7.381	9.42e-13	***
Others - New == 0	1.3174	0.2638	4.995	3.53e-06	***

---

```
Signif. codes:  0 `***' 0.001 `**' 0.01 `*' 0.05 `.' 0.1 ` ' 1  
(Adjusted p values reported -- bonferroni method)
```

# Westfall correction

```
> summary(glht(dative.lmer.access, linfct = K), test = adjusted(`Westfall`))
```

## Simultaneous Tests for General Linear Hypotheses

```
Fit: glmer(formula = RealizationOfRecipient ~ -1 + AccessOfTheme +  
(0 + AccessOfTheme | Verb), data = dative, family = `binomial`)
```

### Linear Hypotheses:

	Estimate	Std. Error	z value	Pr(> z )
Accessible == 0	-0.8172	0.2900	-2.818	0.0123 *
Given == 0	1.3781	0.3590	3.839	<0.001 ***
New == 0	-1.0370	0.3660	-2.833	0.0123 *
Accessible - New == 0	0.2198	0.2646	0.831	0.4061
Given - New == 0	2.4151	0.3272	7.381	<0.001 ***
Others - New == 0	1.3174	0.2638	4.995	<0.001 ***

---

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
(Adjusted p values reported -- Westfall method)
```